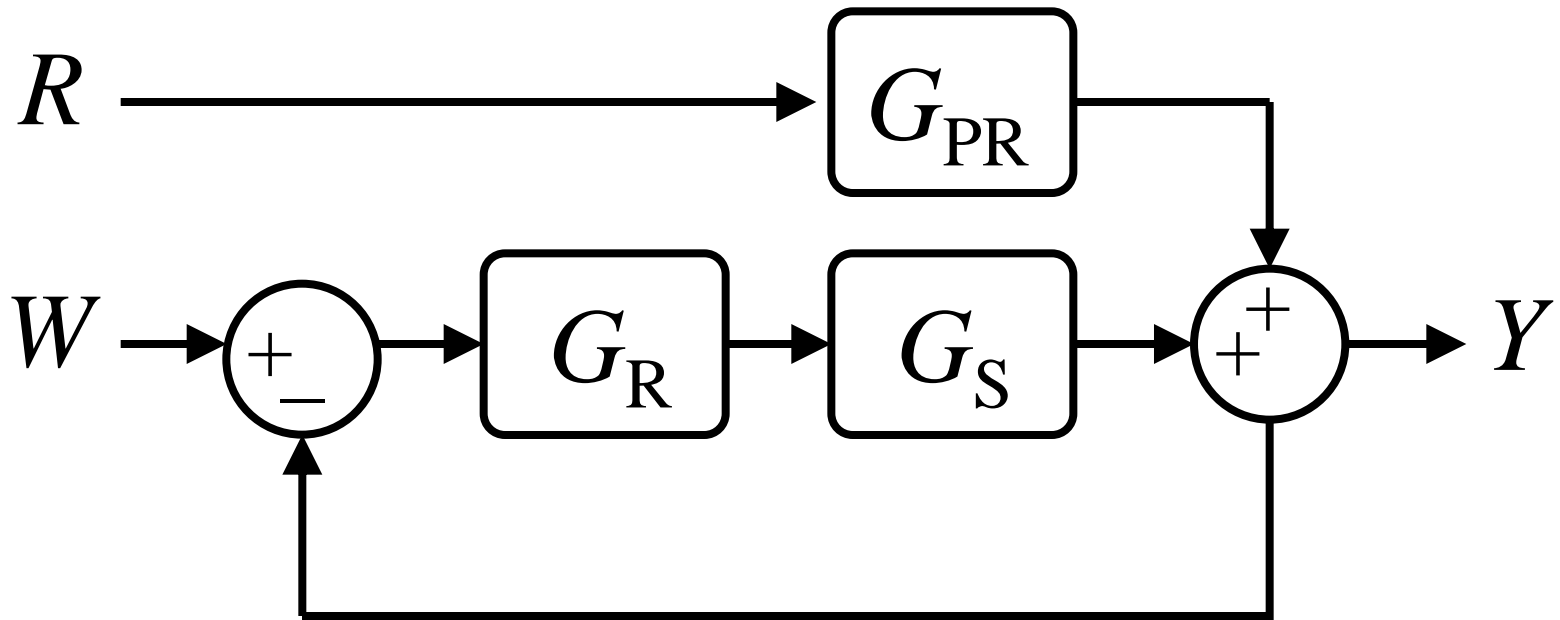


# **PID regulátor**

**Juraj Oravec**

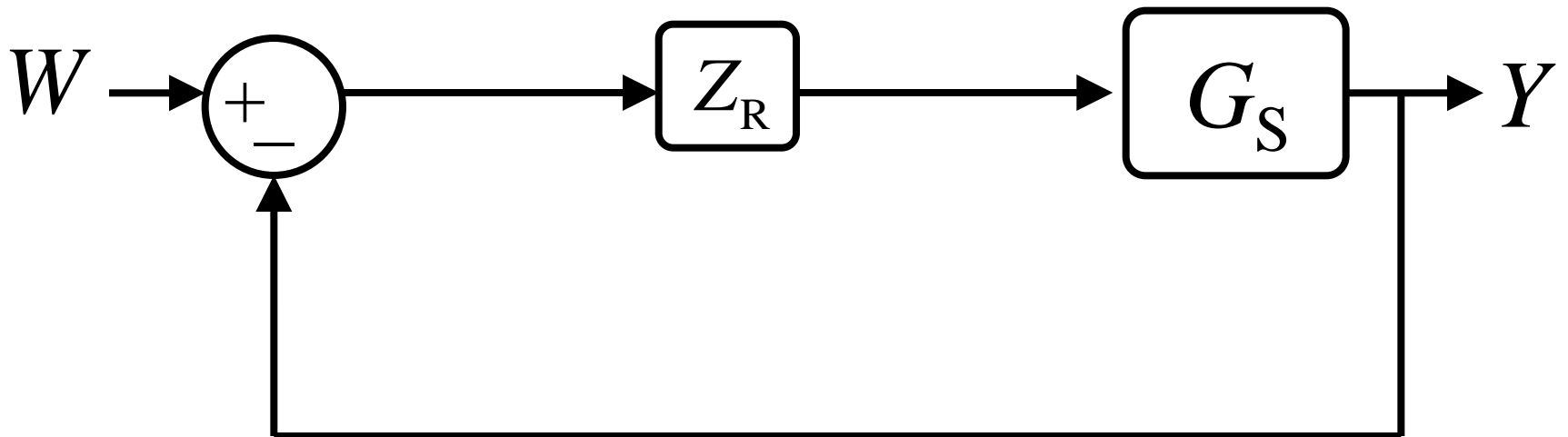
# URO



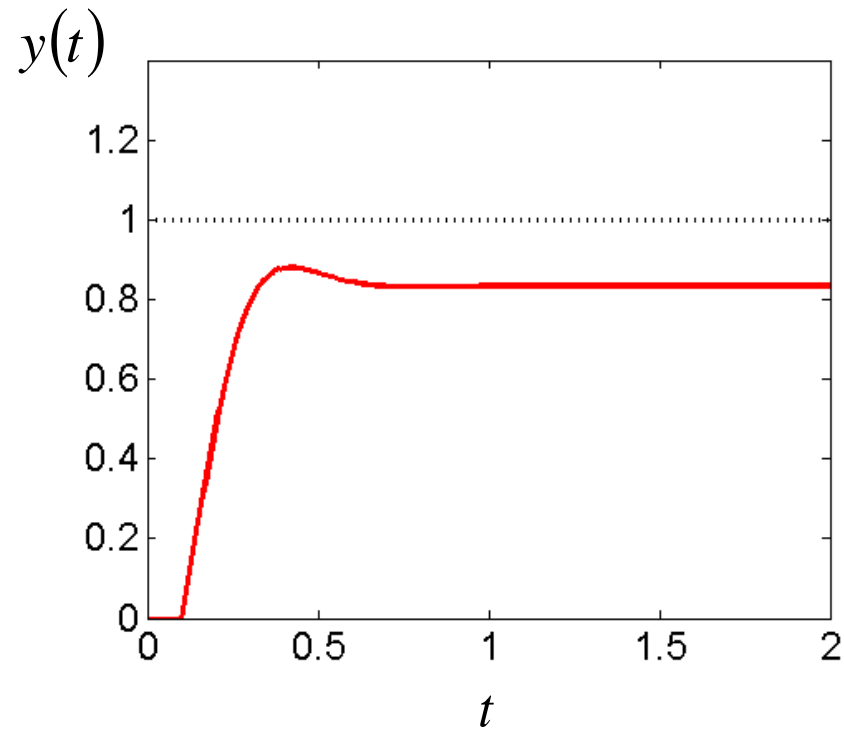
## P – regulátor

$$u(t) = u_P(t)$$

$$u(t) = Z_R e(t)$$

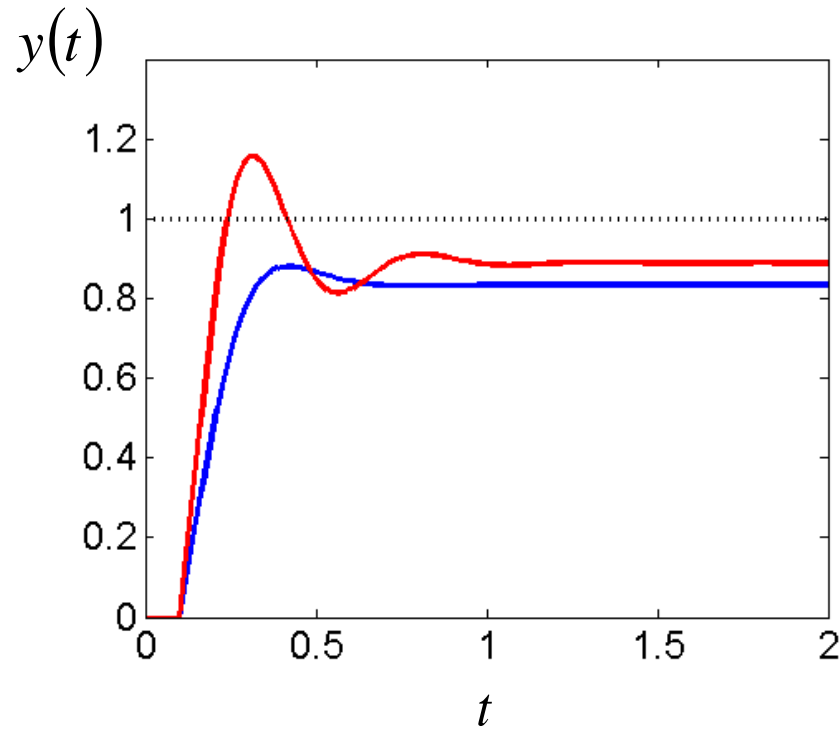


# P – regulátor



$$Z_{R,1} = 5$$

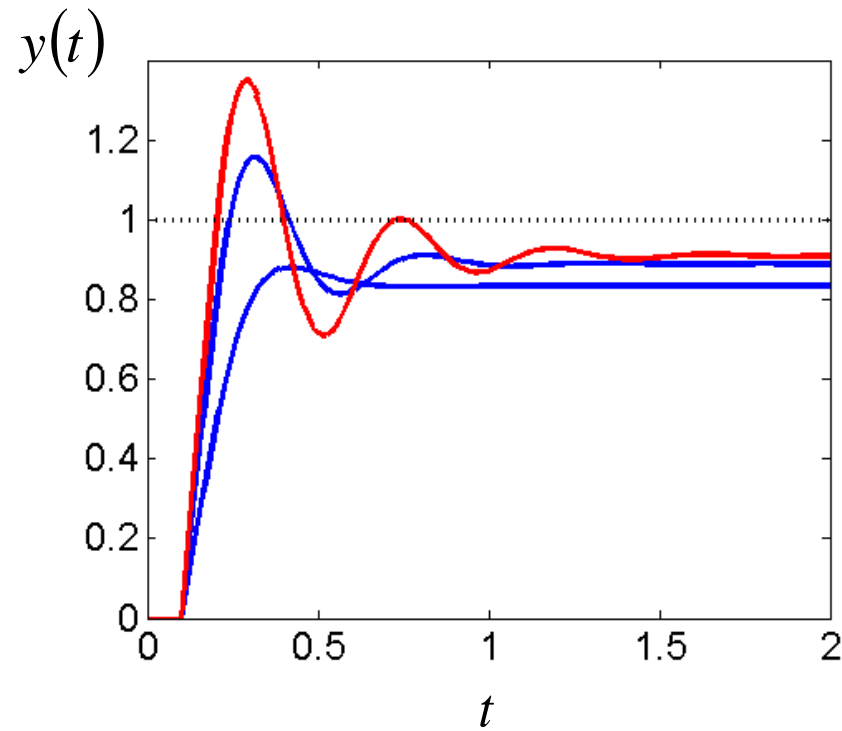
# P – regulátor



$$Z_{R,2} = 8$$

$$Z_{R,1} = 5$$

# P – regulátor

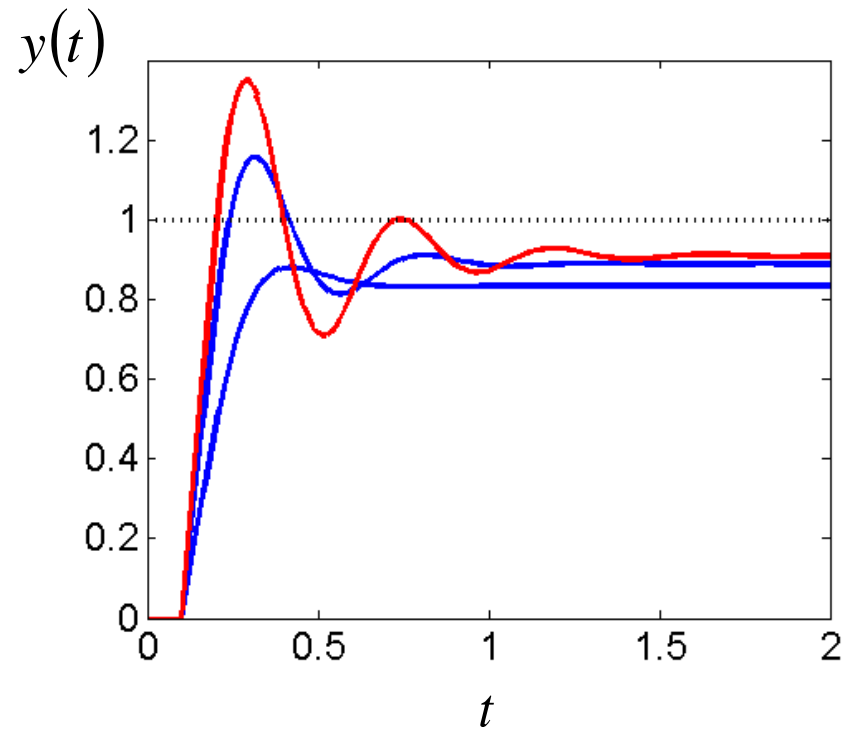


$$Z_{R,3} = 10$$

$$Z_{R,2} = 8$$

$$Z_{R,1} = 5$$

# P – regulátor



$$Z_{R,3} = 10$$

$$Z_{R,2} = 8$$

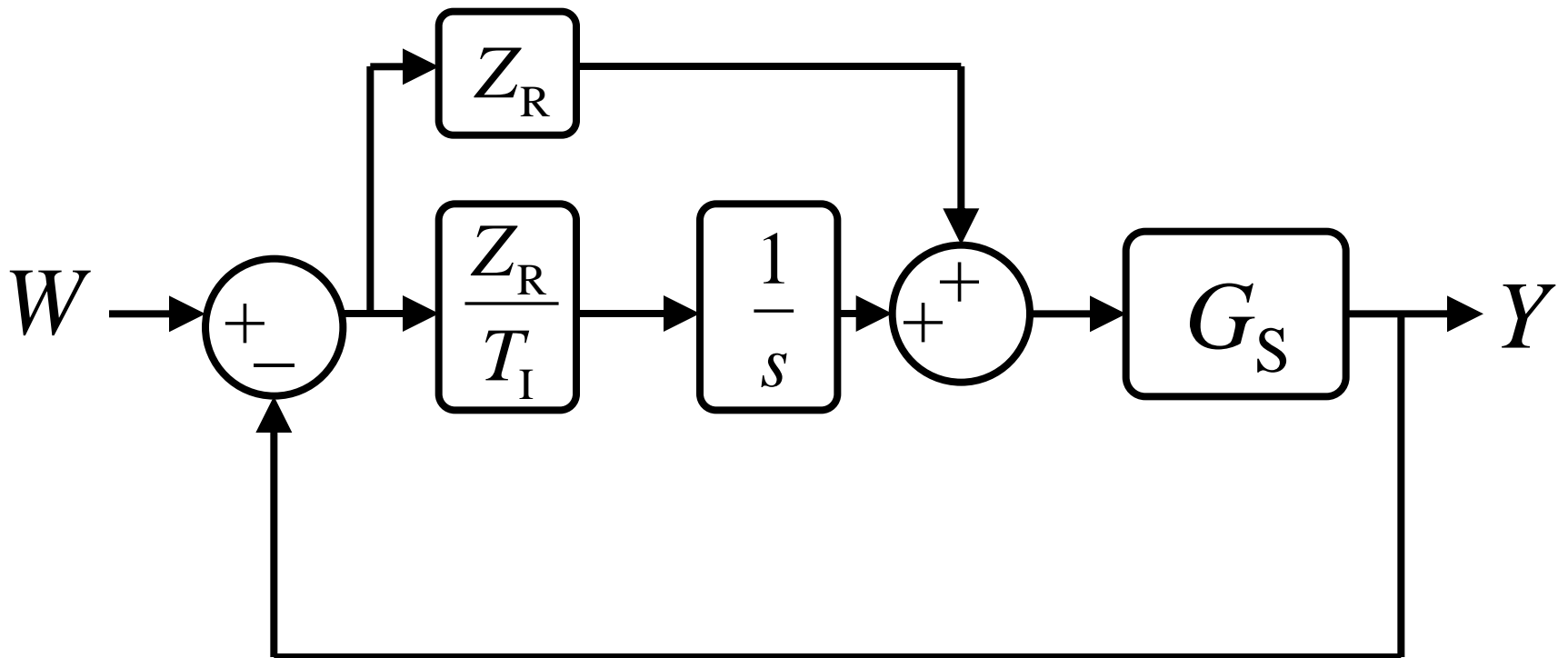
$$Z_{R,1} = 5$$

$\uparrow Z_R \Rightarrow \downarrow TRO, \uparrow \sigma_{\max}$

## PI – regulátor

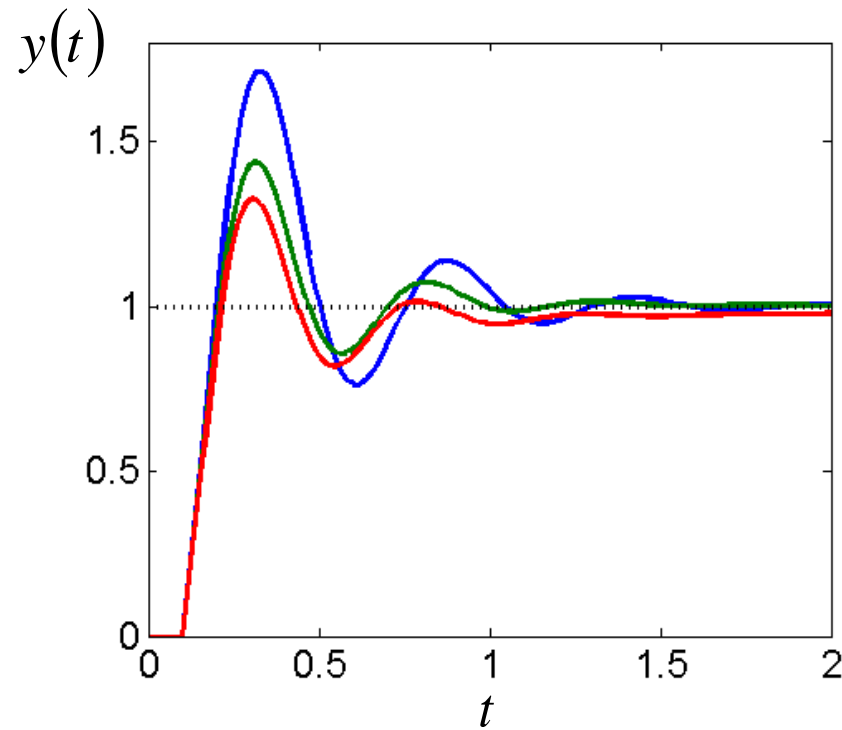
$$u(t) = u_P(t) + u_I(t)$$

$$u(t) = Z_R e(t) + \frac{Z_R}{T_I} \int_0^t e(\tau) d\tau$$





# PI – regulátor



$$T_{I,1} = 0,3$$

$$T_{I,2} = 0,8$$

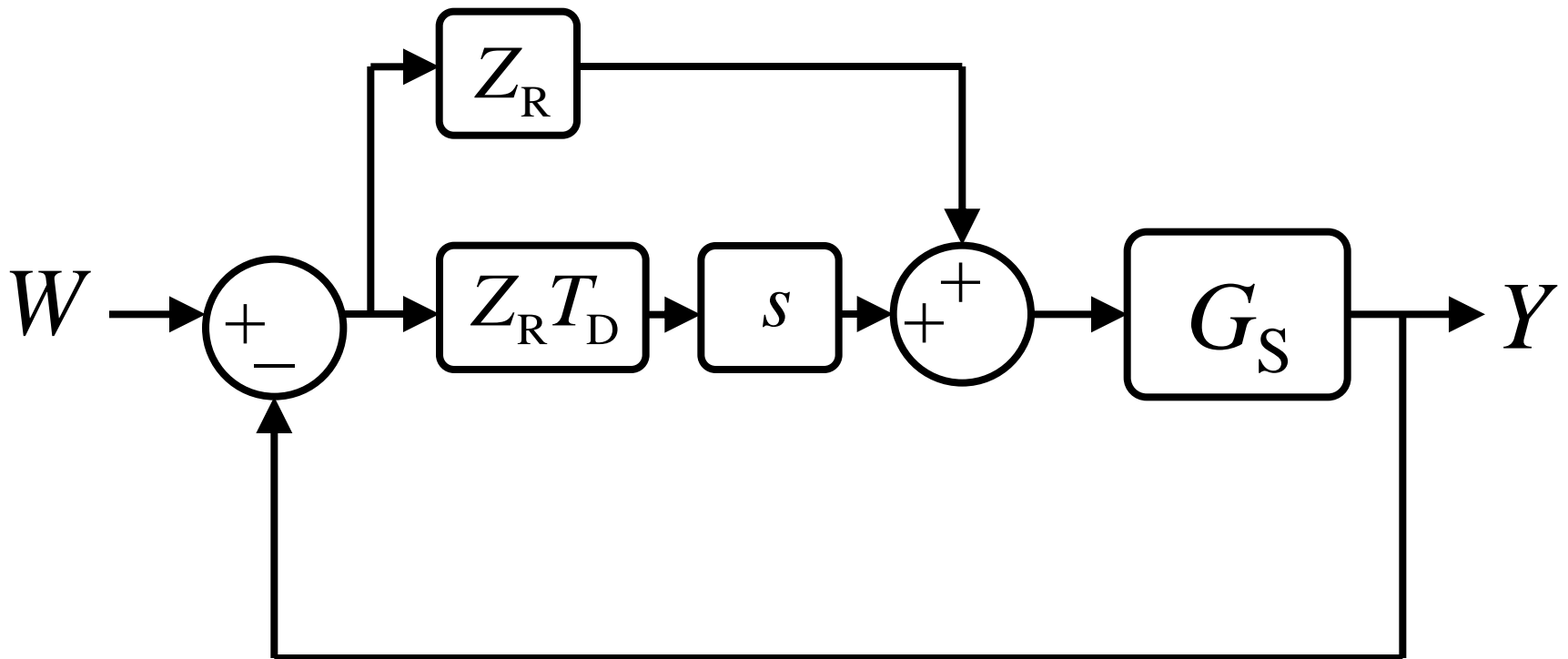
$$T_{I,3} = 2,0$$

$$\uparrow T_I \Rightarrow \downarrow t_{\text{reg}}, \downarrow \sigma_{\text{max}}$$

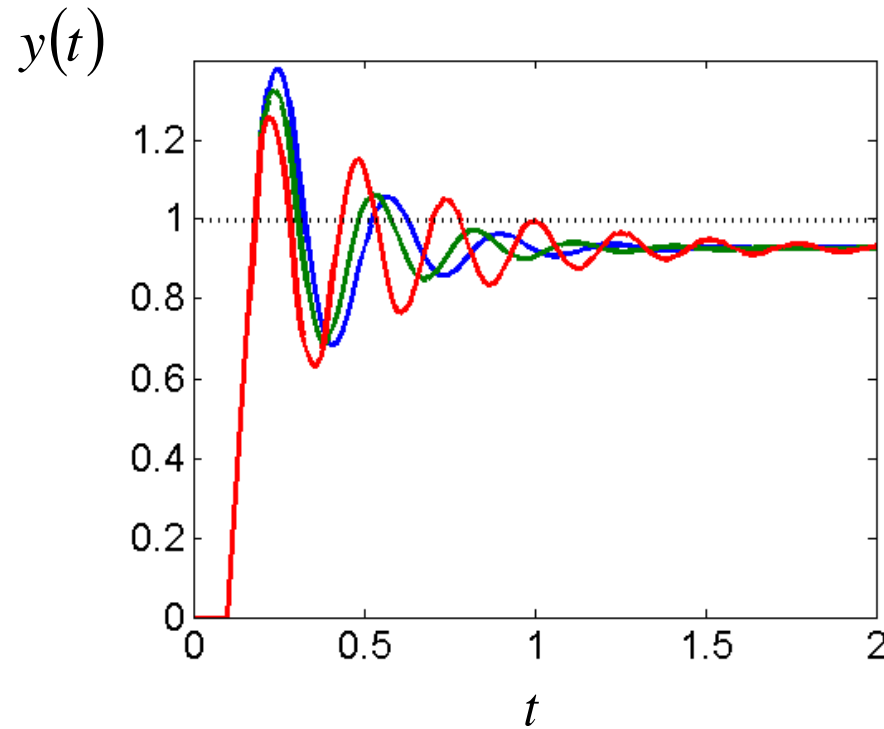
## PD – regulátor

$$u(t) = u_P(t) + u_D(t)$$

$$u(t) = Z_R e(t) + Z_R T_D \frac{de(t)}{dt}$$



# PD – regulátor



$$T_{D,1} = 0,025$$

$$T_{D,2} = 0,035$$

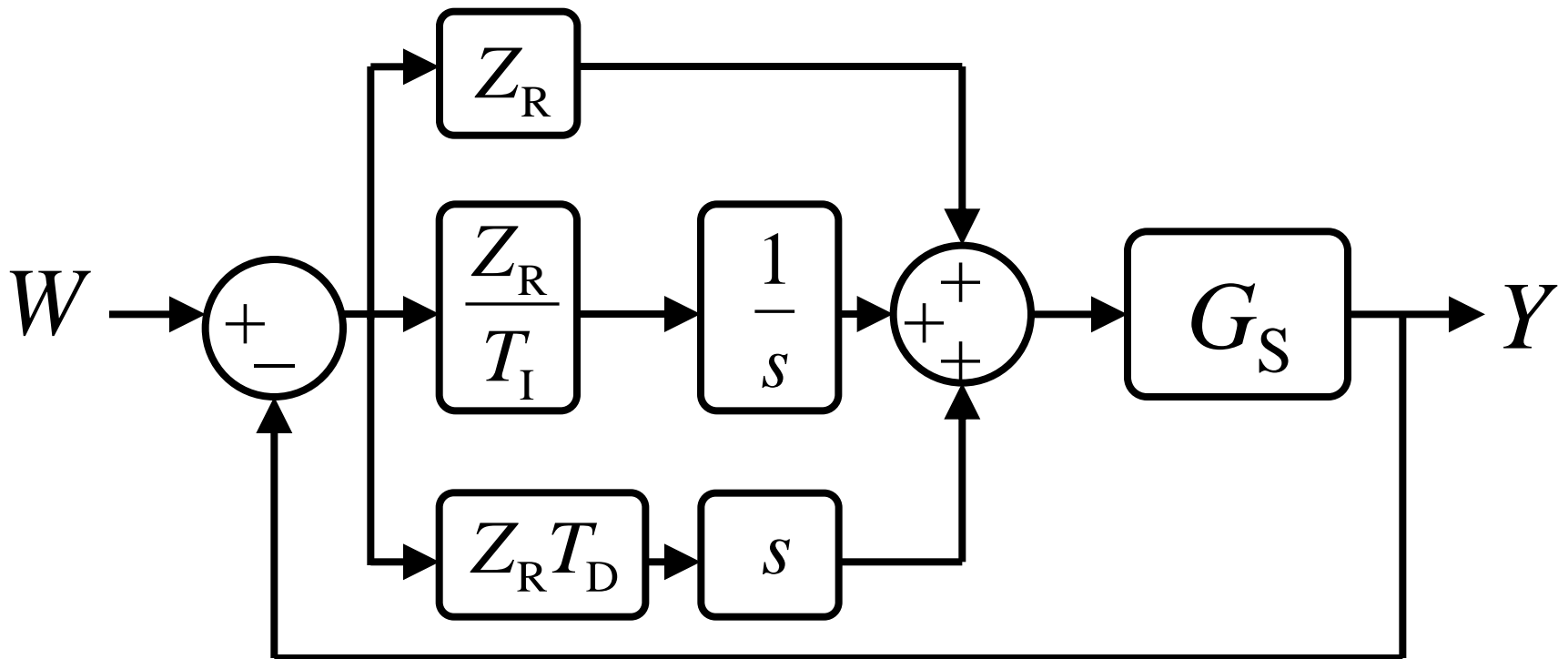
$$T_{D,3} = 0,050$$

$$\uparrow T_D \Rightarrow \uparrow t_{\text{reg}}, \downarrow \sigma_{\text{max}}$$

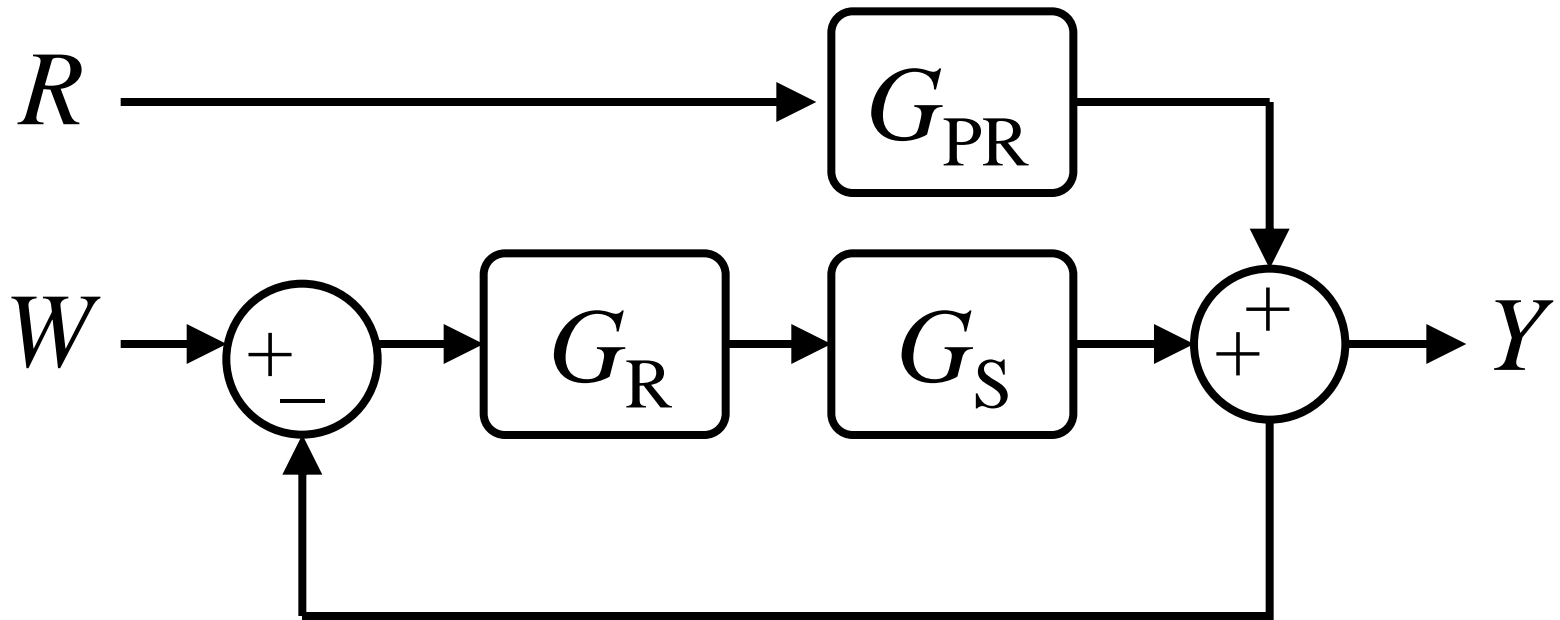
# PID – regulátor

$$u(t) = u_P(t) + u_I(t) + u_D(t)$$

$$u(t) = Z_R e(t) + \frac{Z_R}{T_I} \int_0^t e(\tau) d\tau + Z_R T_D \frac{de(t)}{dt}$$



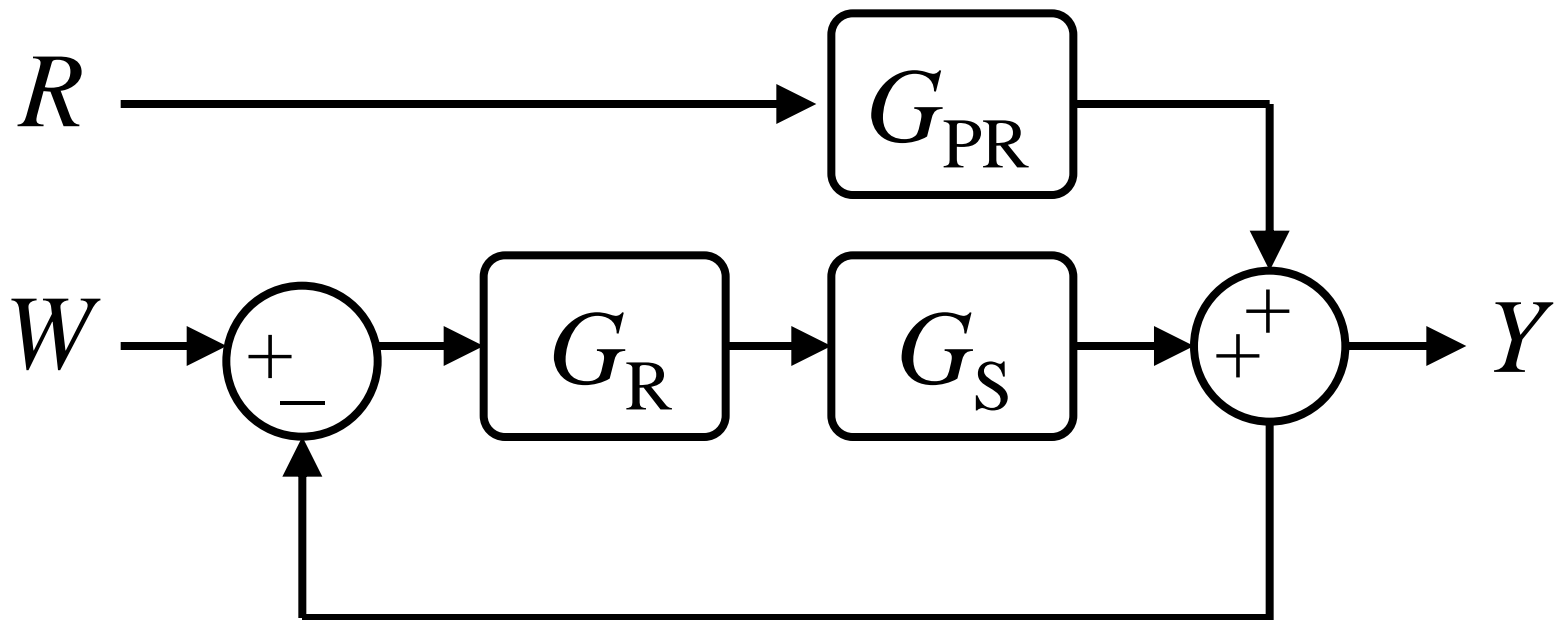
# URO



# Úloha sledovania

$$W \neq 0$$

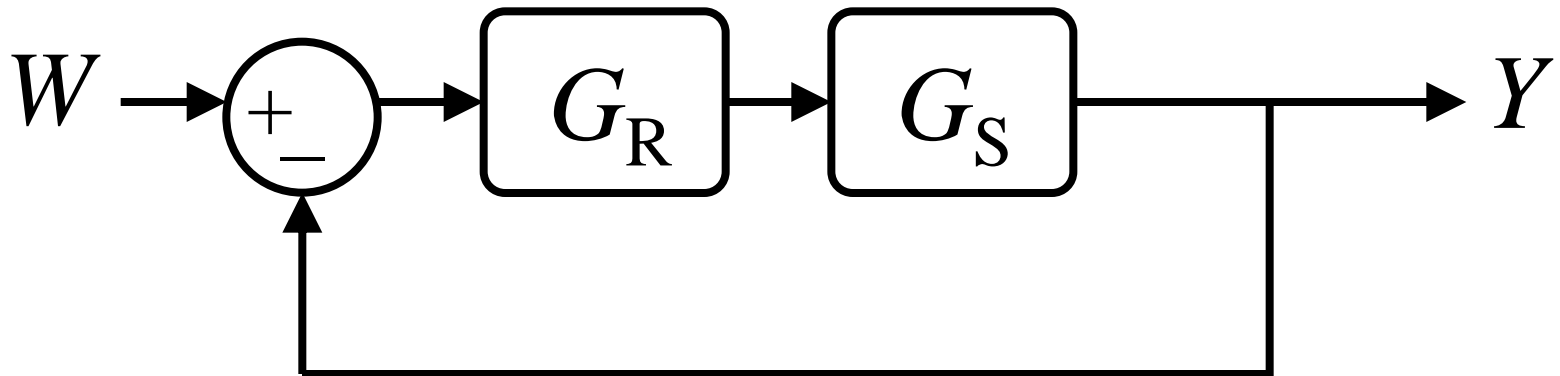
$$R = 0$$



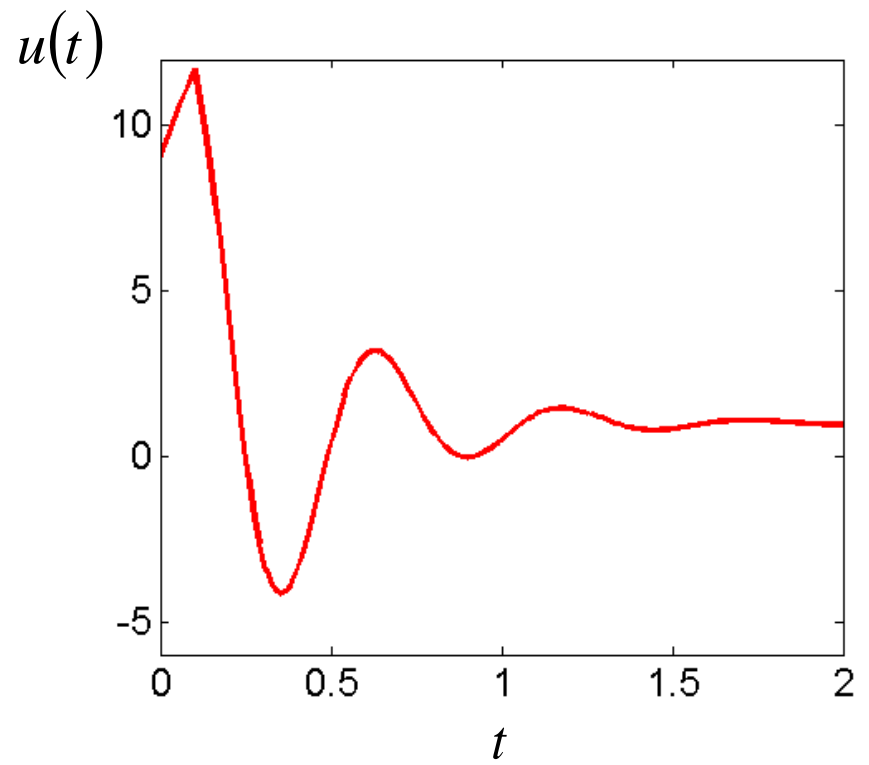
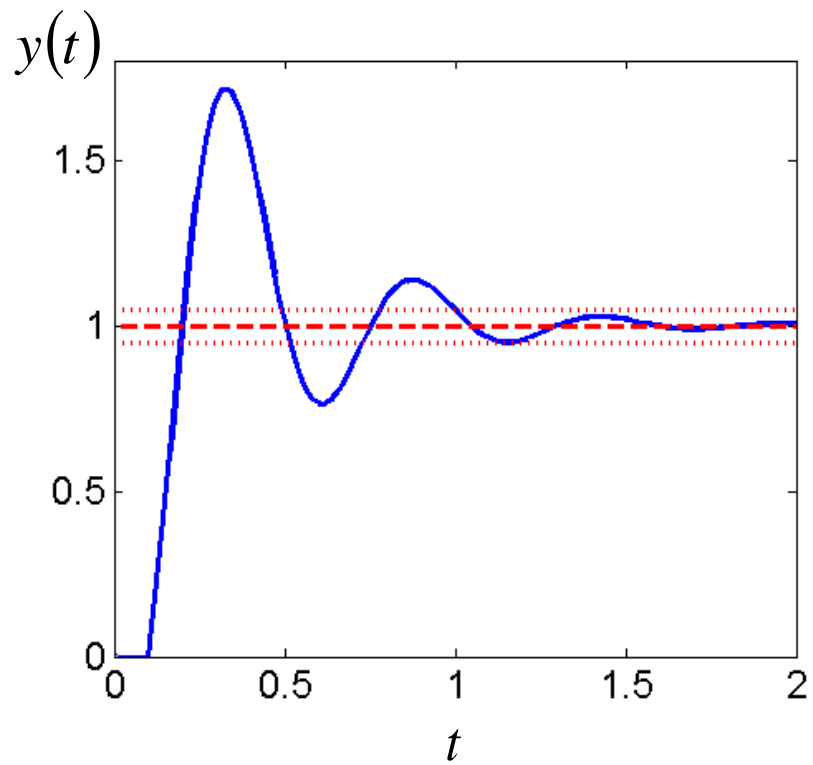
# Úloha sledovania

$$W \neq 0$$

$$R = 0$$

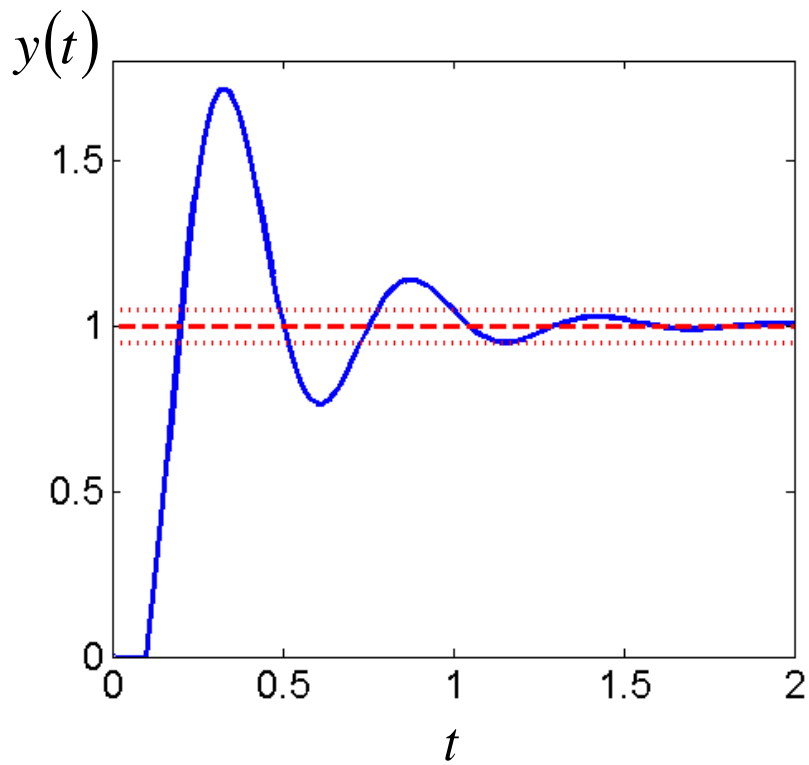


# Úloha sledovania

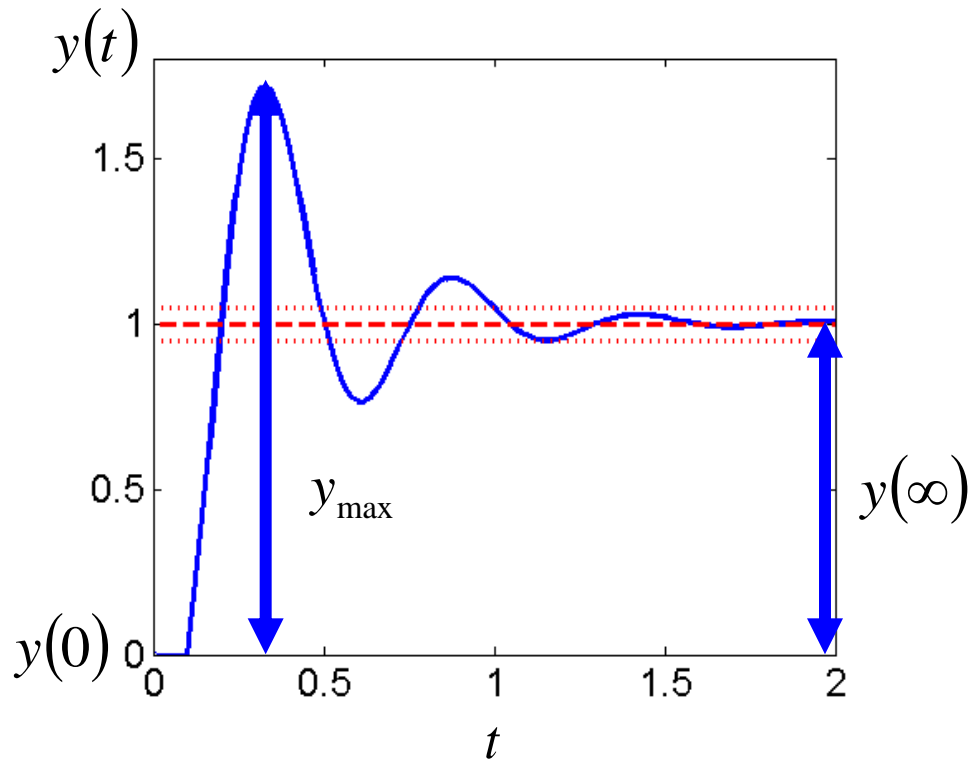




# Kvalita riadenia – kritéria v časovej oblasti

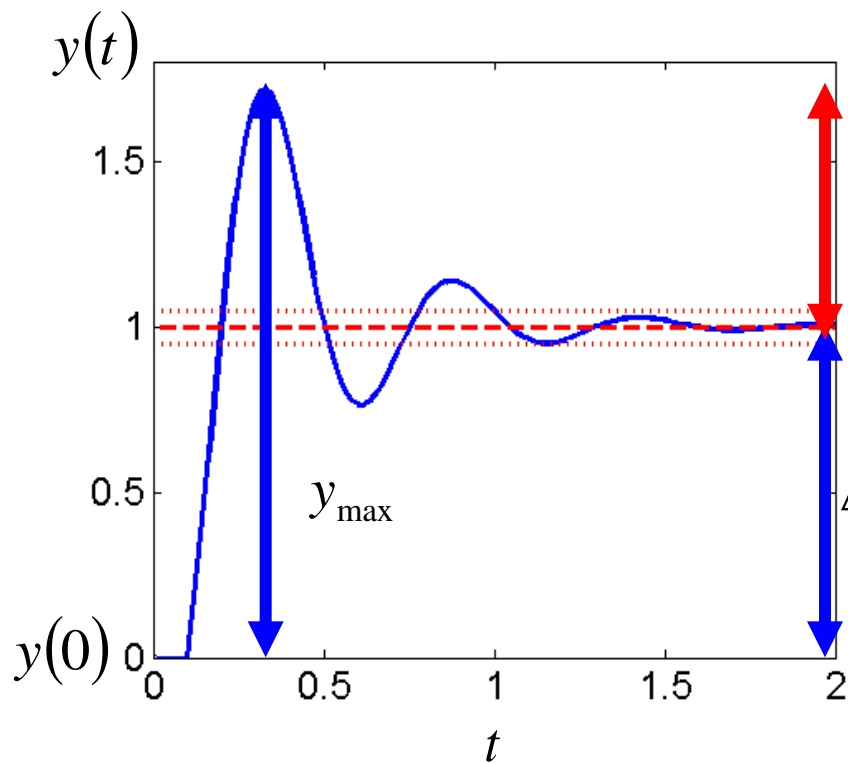


# Kvalita riadenia – maximálne preregulovanie



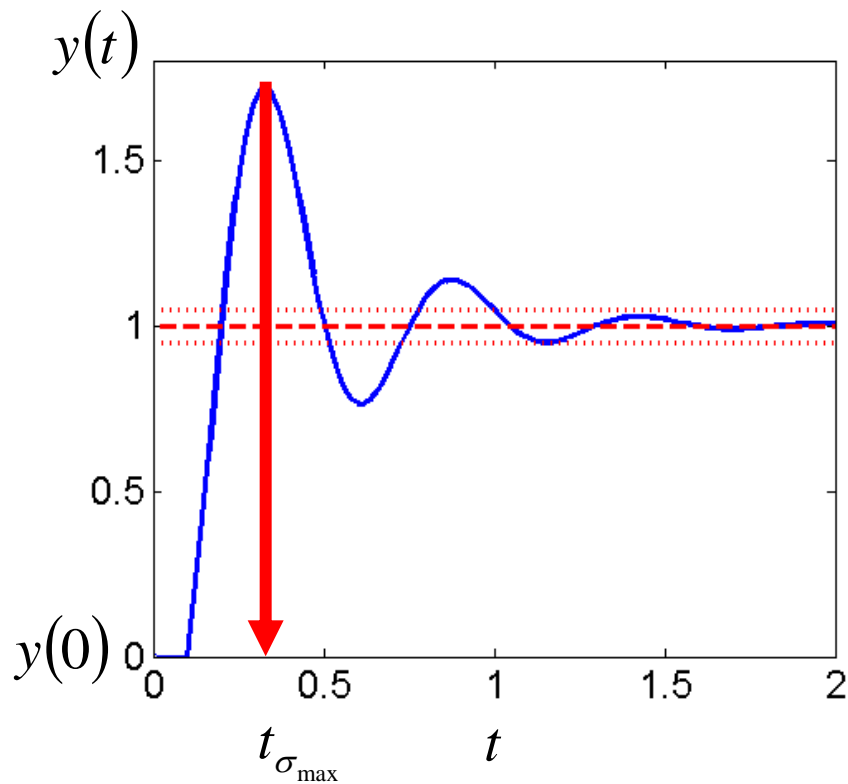
$$\sigma_{\max} = \frac{y_{\max} - y(0)}{y(\infty) - y(0)} \times 100\%$$

# Kvalita riadenia – maximálne preregulovanie



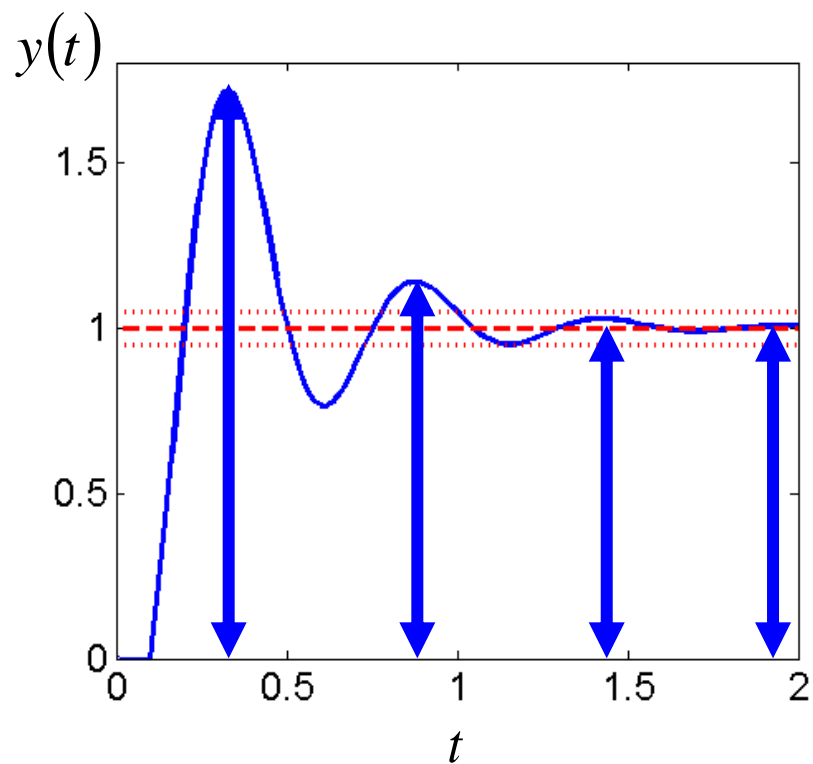
$$\sigma_{\max} = \frac{\Delta y_{\max}}{\Delta y(\infty)} \times 100\%$$

# Kvalita riadenia – čas maximálneho preregulovania

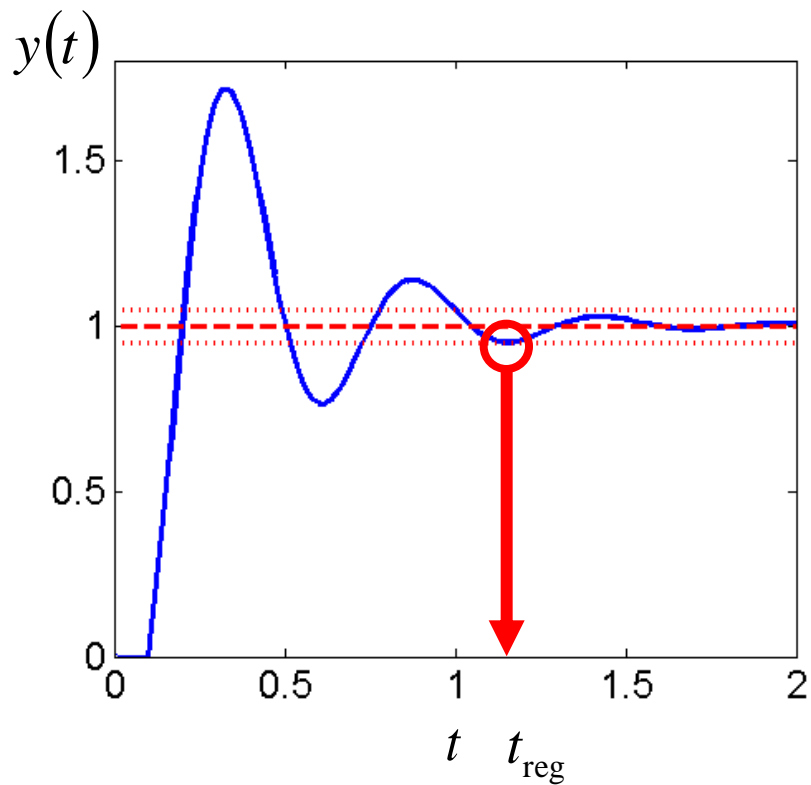


$$t_{\sigma_{\max}} = \{t : y(t) = y_{\max}\}$$

# Kvalita riadenia – počet preregulovaní

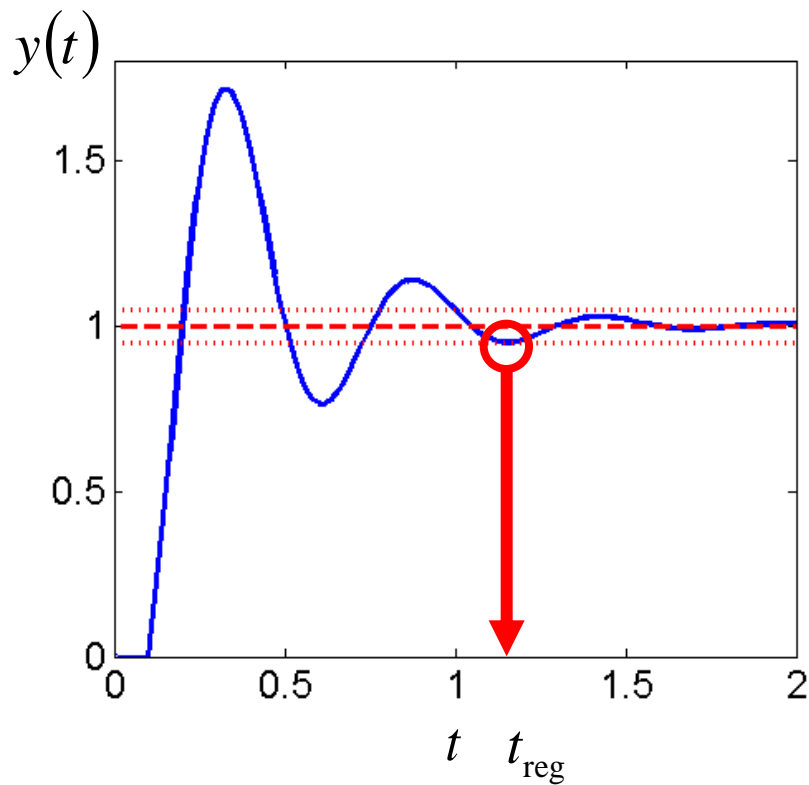


# Kvalita riadenia – čas regulácie

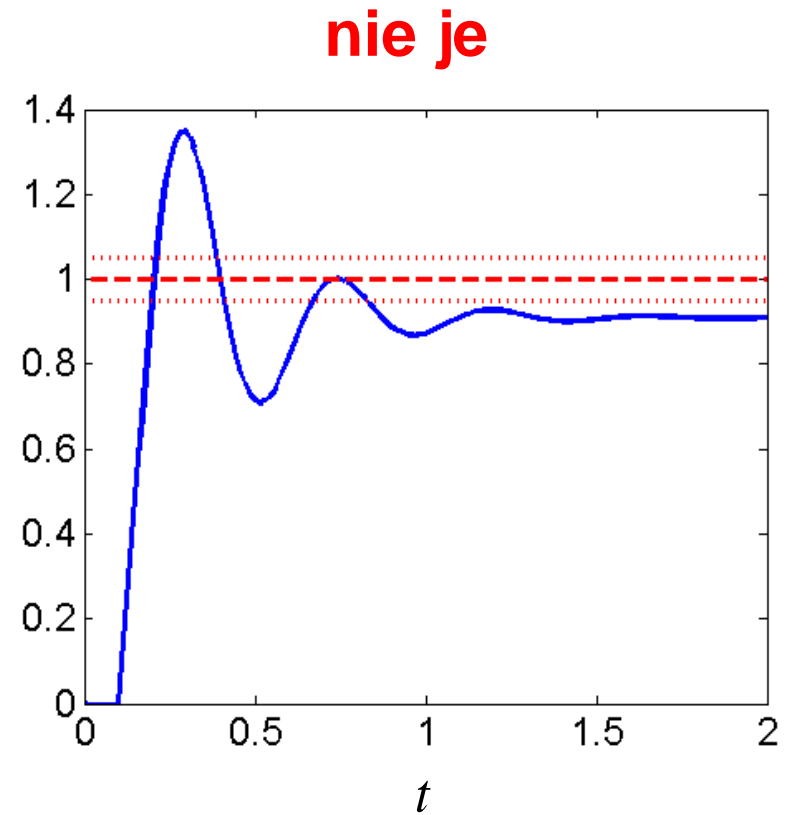


$$y(t) \in \langle w - \delta, w + \delta \rangle \quad t > t_{\text{reg}}$$

# Kvalita riadenia – čas regulácie

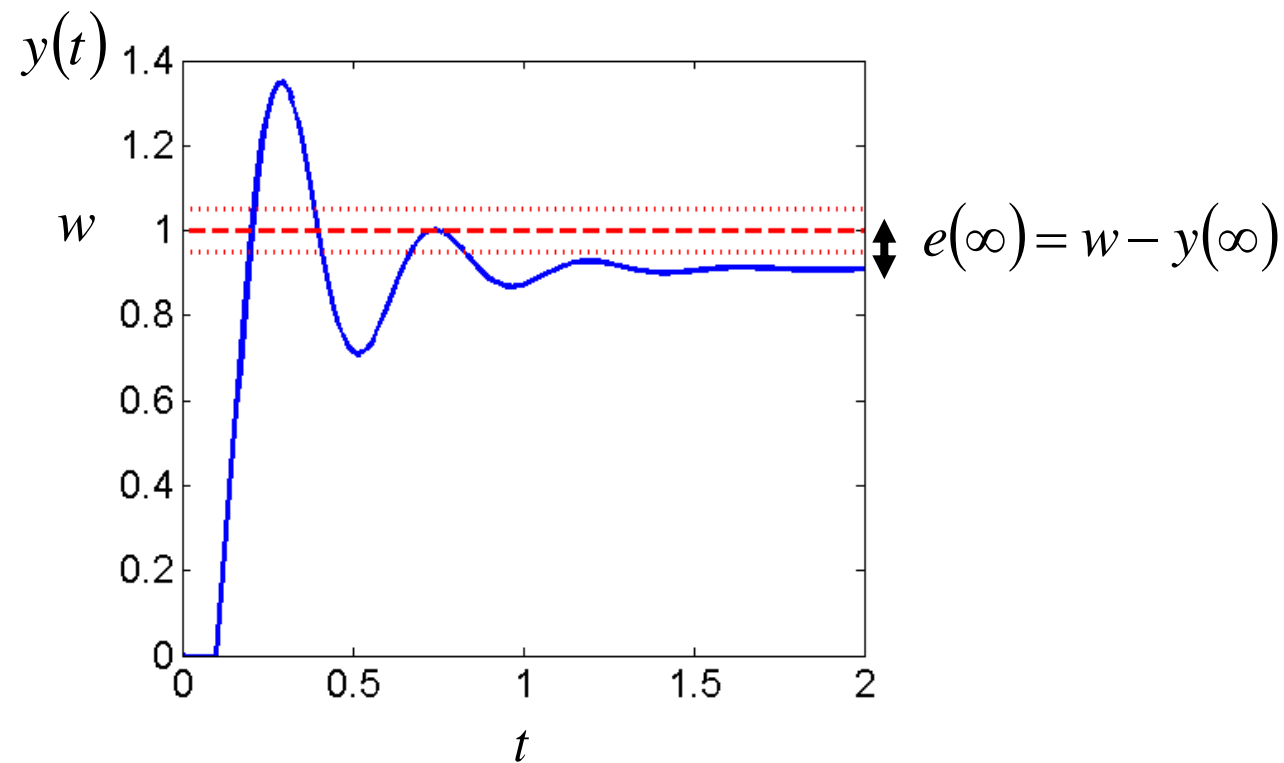


$$y(t) \in \langle w - \delta, w + \delta \rangle \quad t > t_{\text{reg}}$$



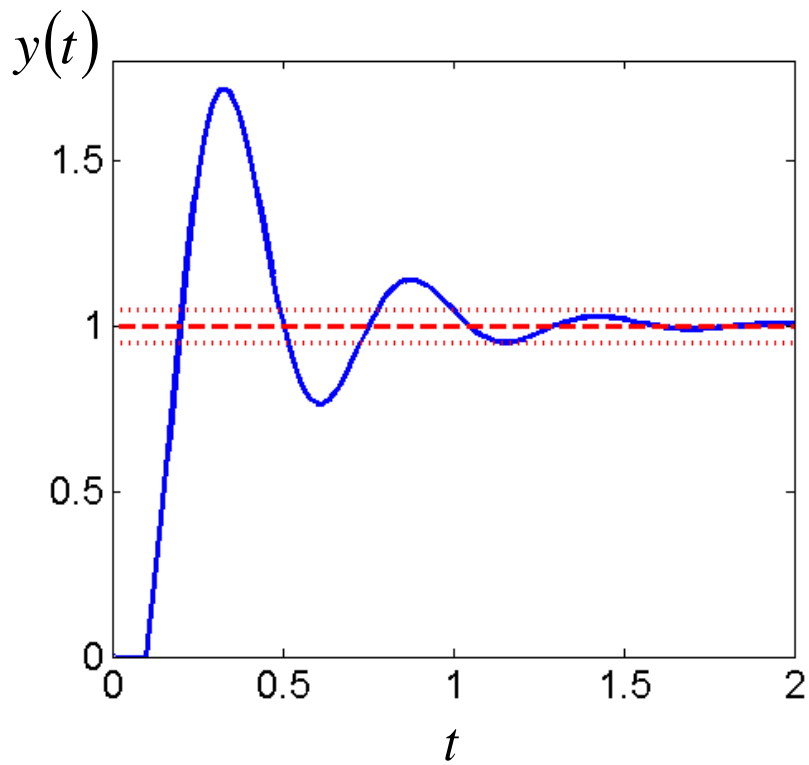
$$y(\infty) \notin \langle w - \delta, w + \delta \rangle$$

# Kvalita riadenia – trvalá regulačná odchýlka

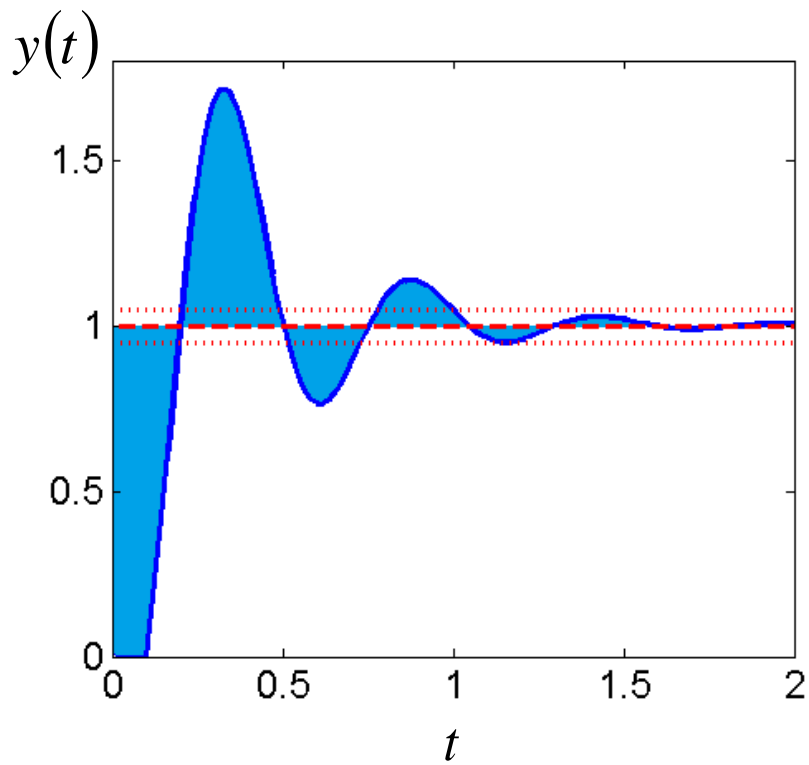




# Kvalita riadenia – integrálne kritéria

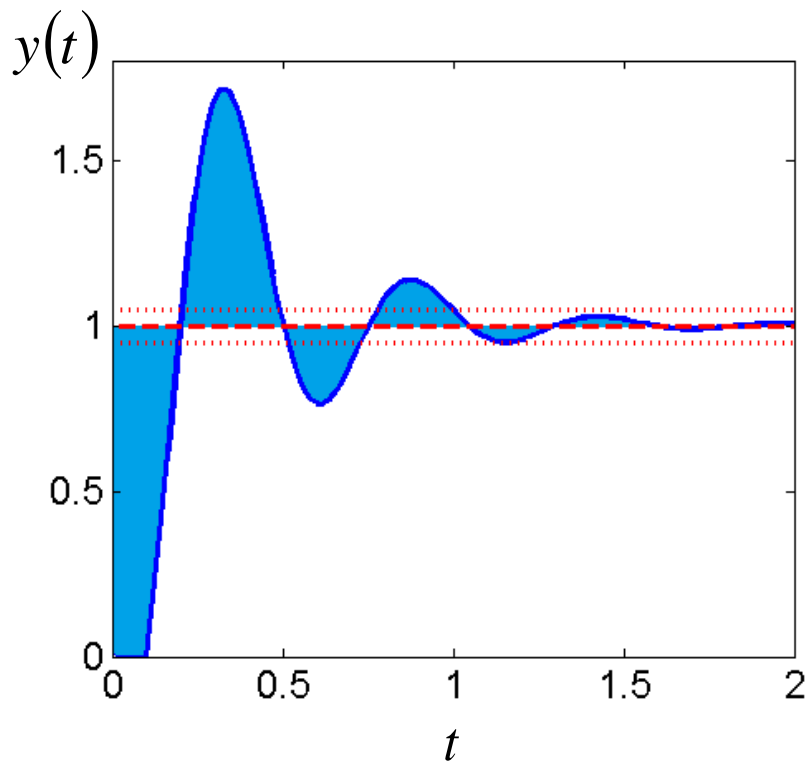


# Kvalita riadenia – IAE



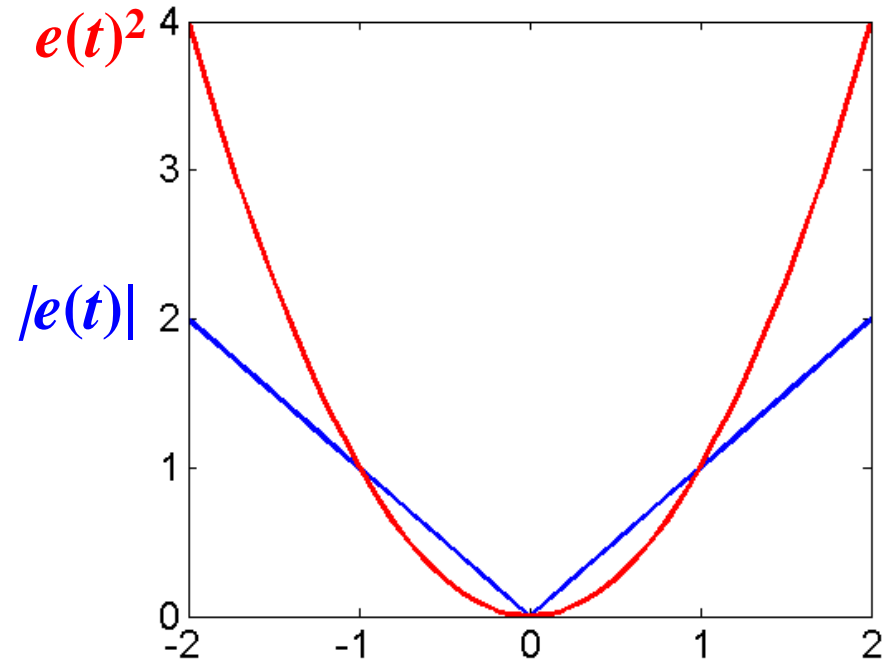
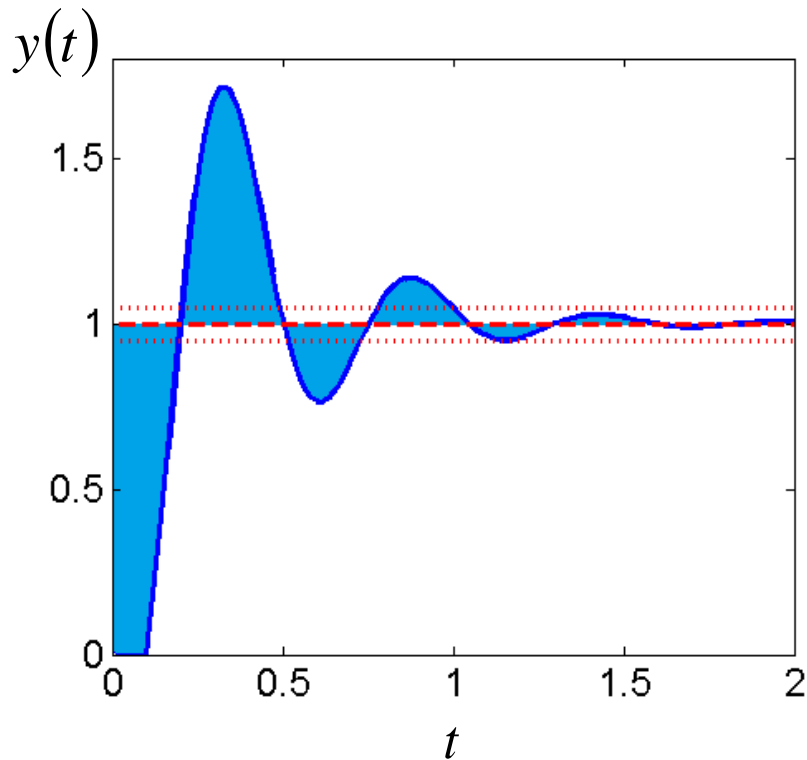
$$IAE = \int_0^{\infty} |e(t)| dt$$

# Kvalita riadenia – ISE



$$ISE = \int_0^{\infty} e(t)^2 dt$$

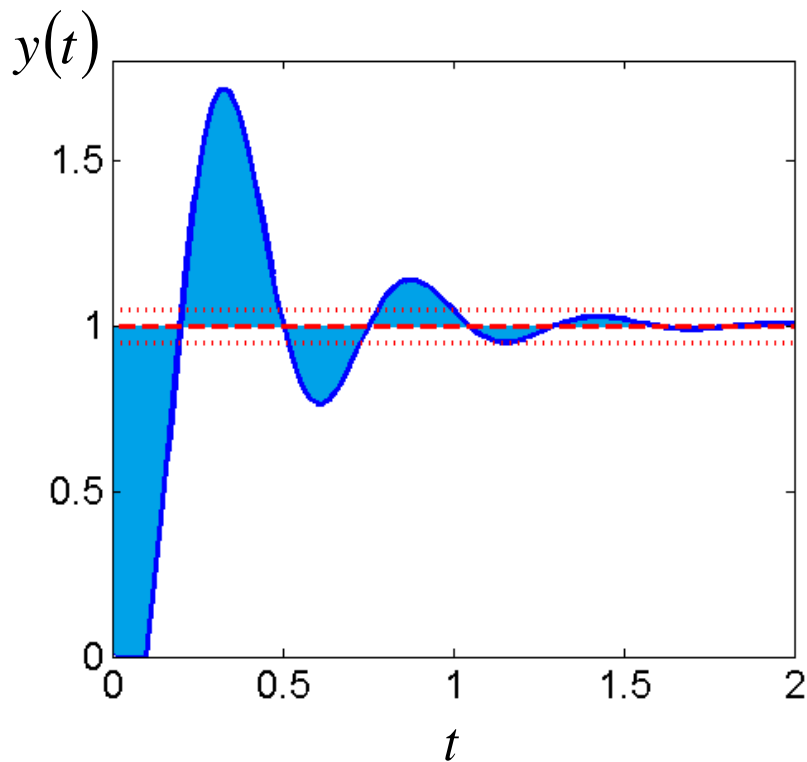
# Kvalita riadenia – IAE vs. ISE



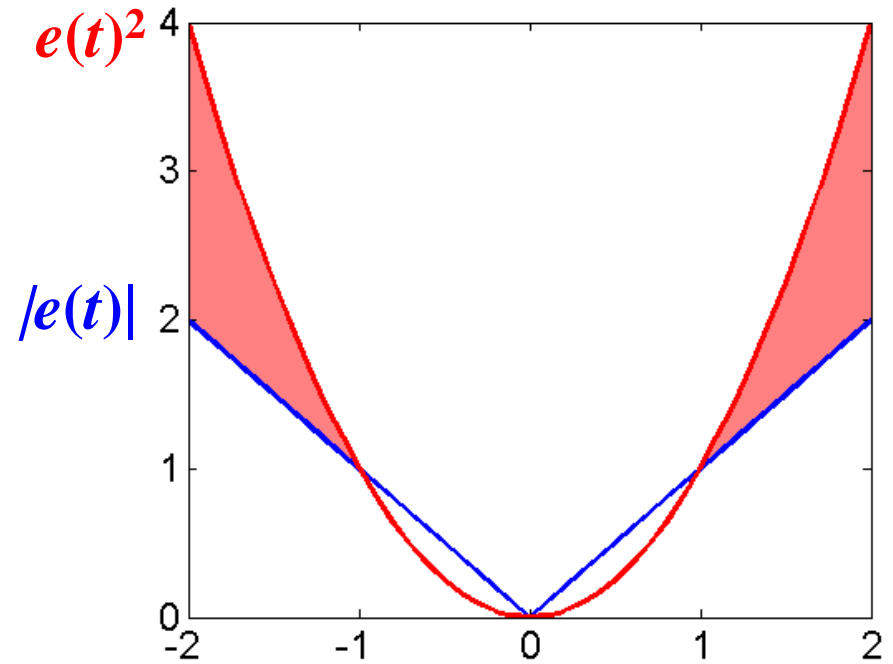
$$IAE = \int_0^{\infty} |e(t)| dt$$

$$ISE = \int_0^{\infty} e(t)^2 dt$$

# Kvalita riadenia – IAE vs. ISE

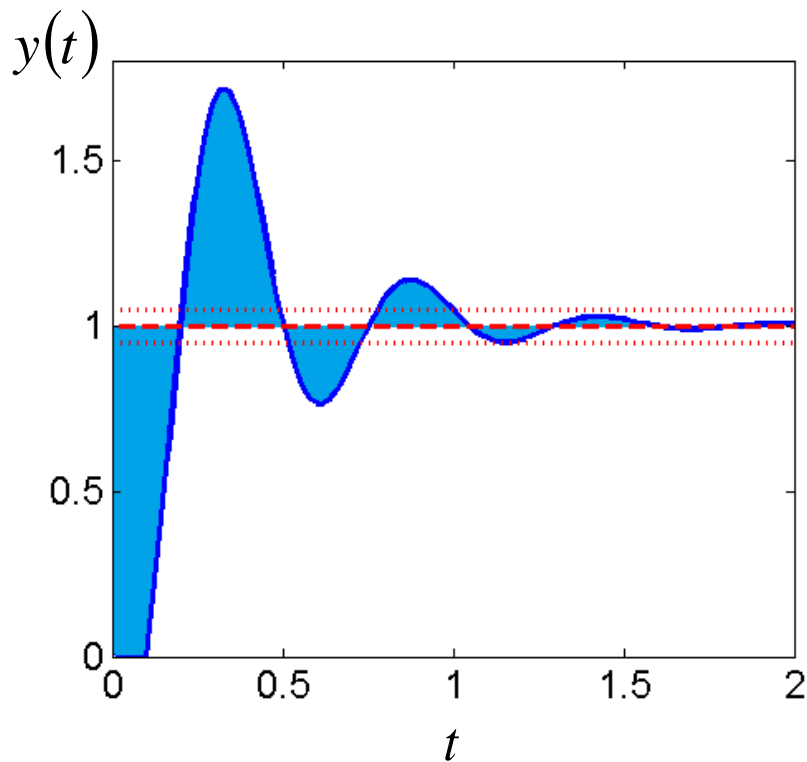


$$IAE = \int_0^{\infty} |e(t)| dt$$

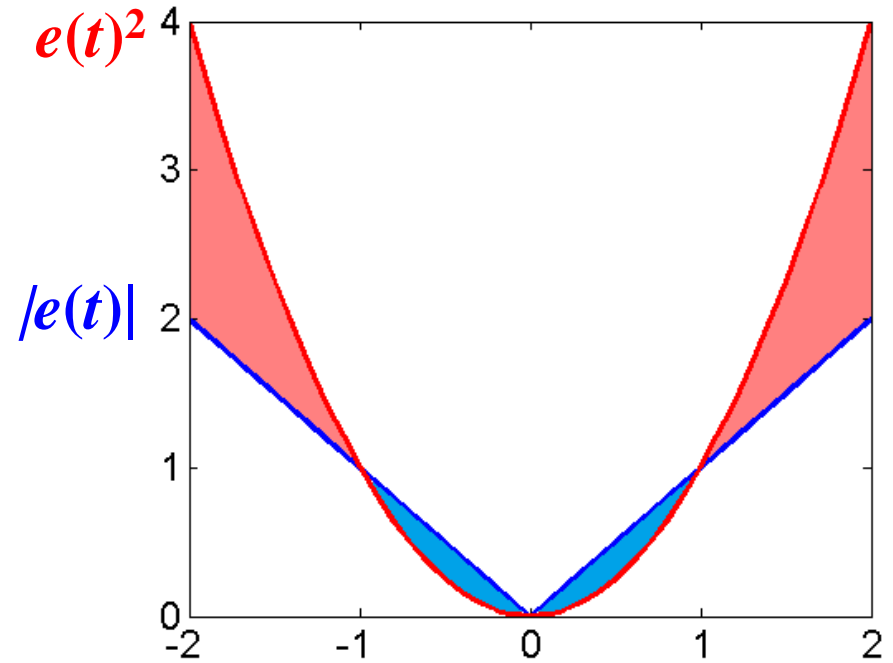


$$ISE = \int_0^{\infty} e(t)^2 dt$$

# Kvalita riadenia – IAE vs. ISE

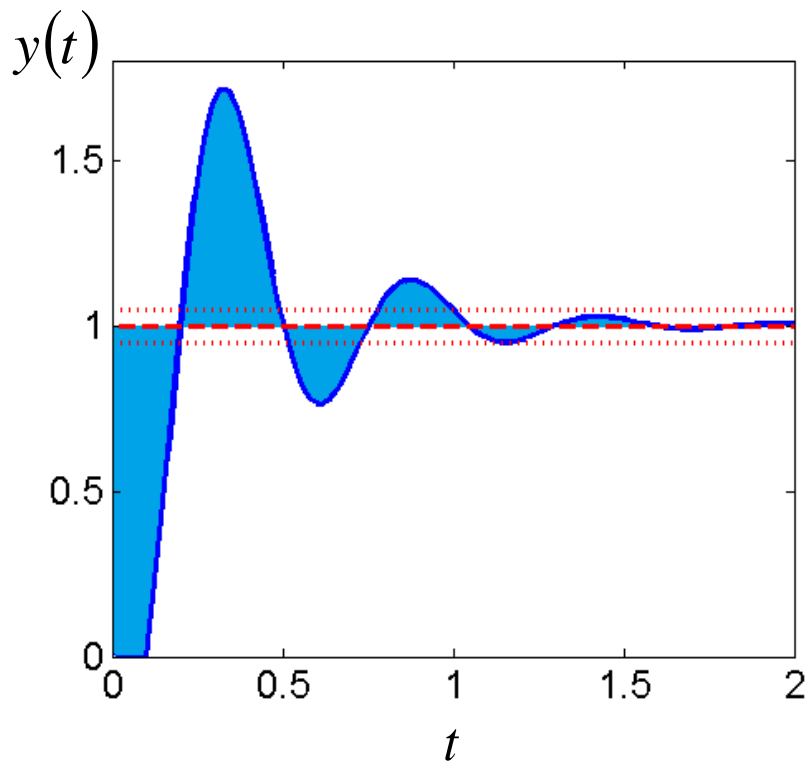


$$IAE = \int_0^{\infty} |e(t)| dt$$



$$ISE = \int_0^{\infty} e(t)^2 dt$$

# Kvalita riadenia – ITAE, ITSE, ISTSE

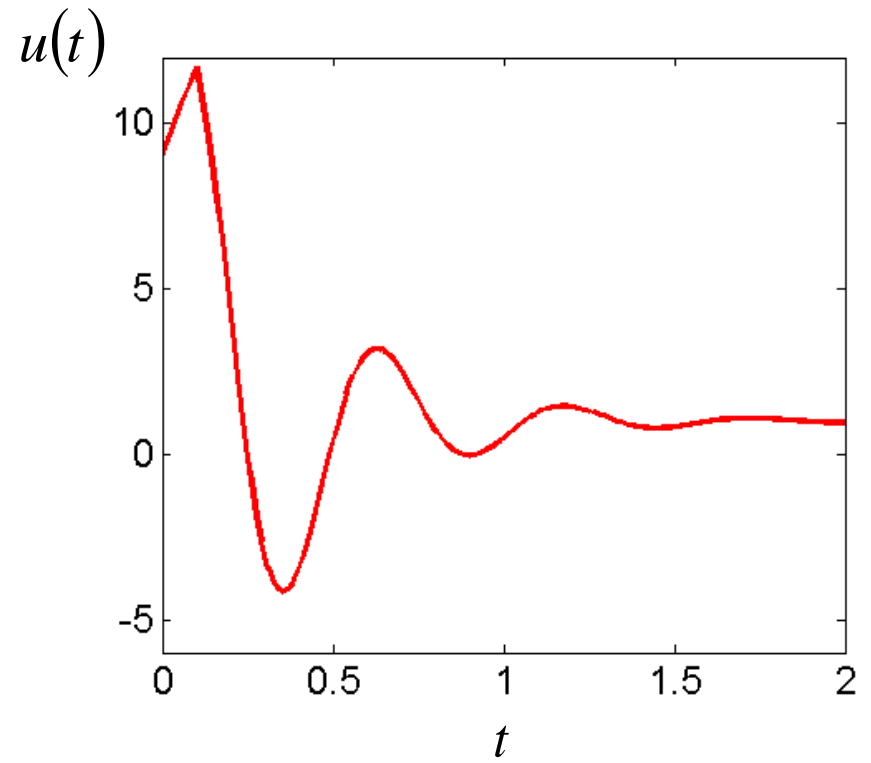
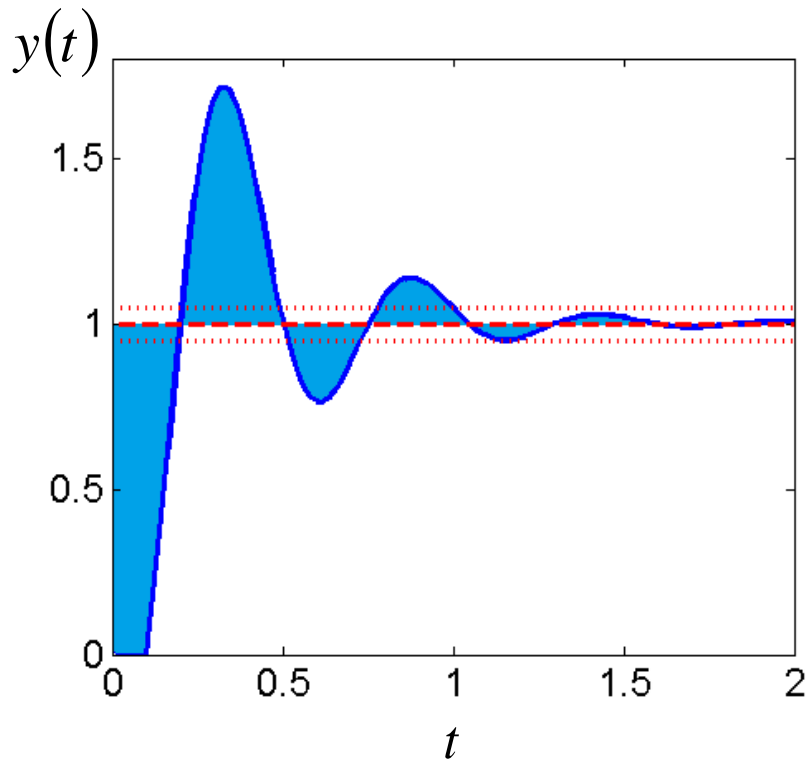


$$ITAE = \int_0^{\infty} t |e(t)| dt$$

$$ITSE = \int_0^{\infty} t e(t)^2 dt$$

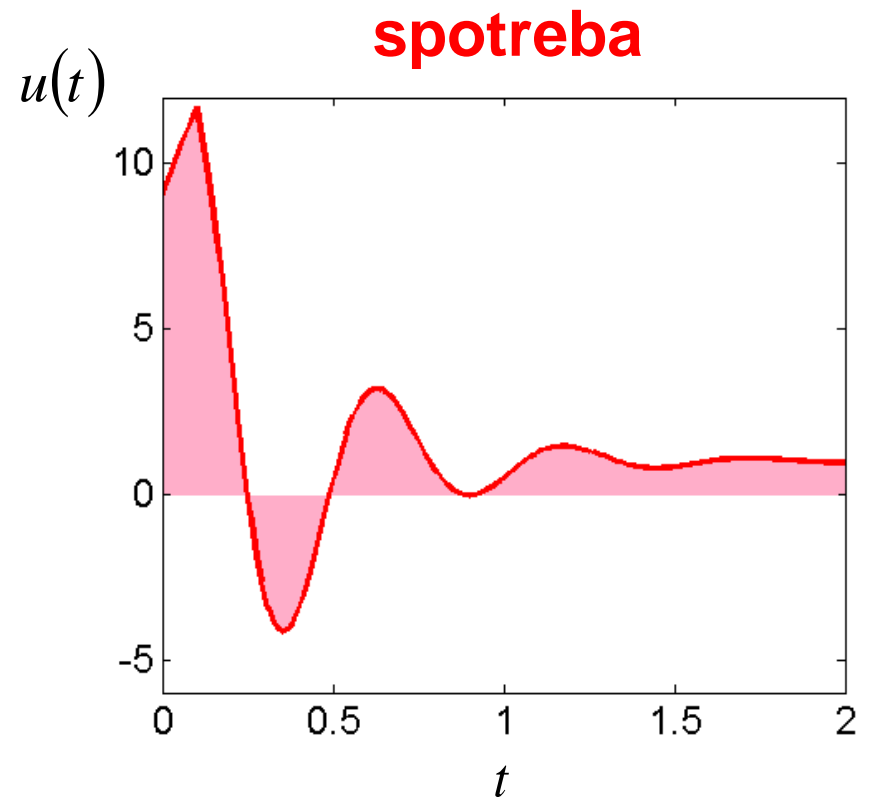
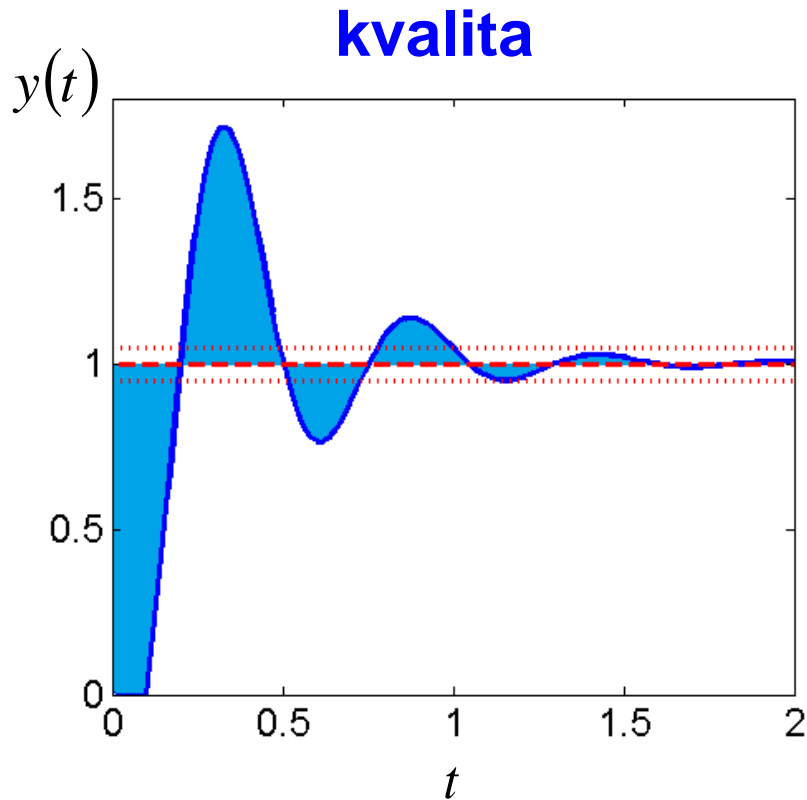
$$ISTSE = \int_0^{\infty} t^2 e(t)^2 dt$$

# Kvalita riadenia – komplexné kritérium





# Kvalita riadenia – komplexné kritérium

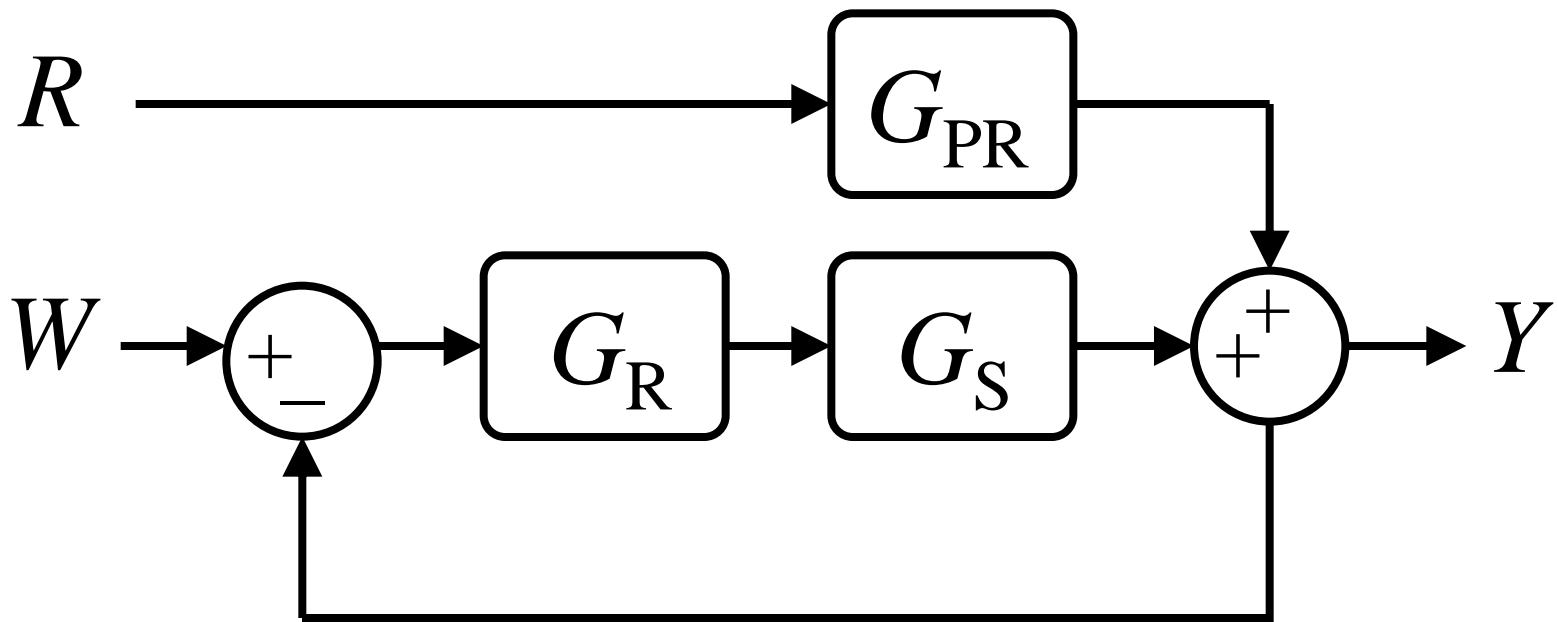


$$J = \int_0^{\infty} (Qe(t)^2 + Ru(t)^2) dt$$

# Úloha regulácie

$$W = 0$$

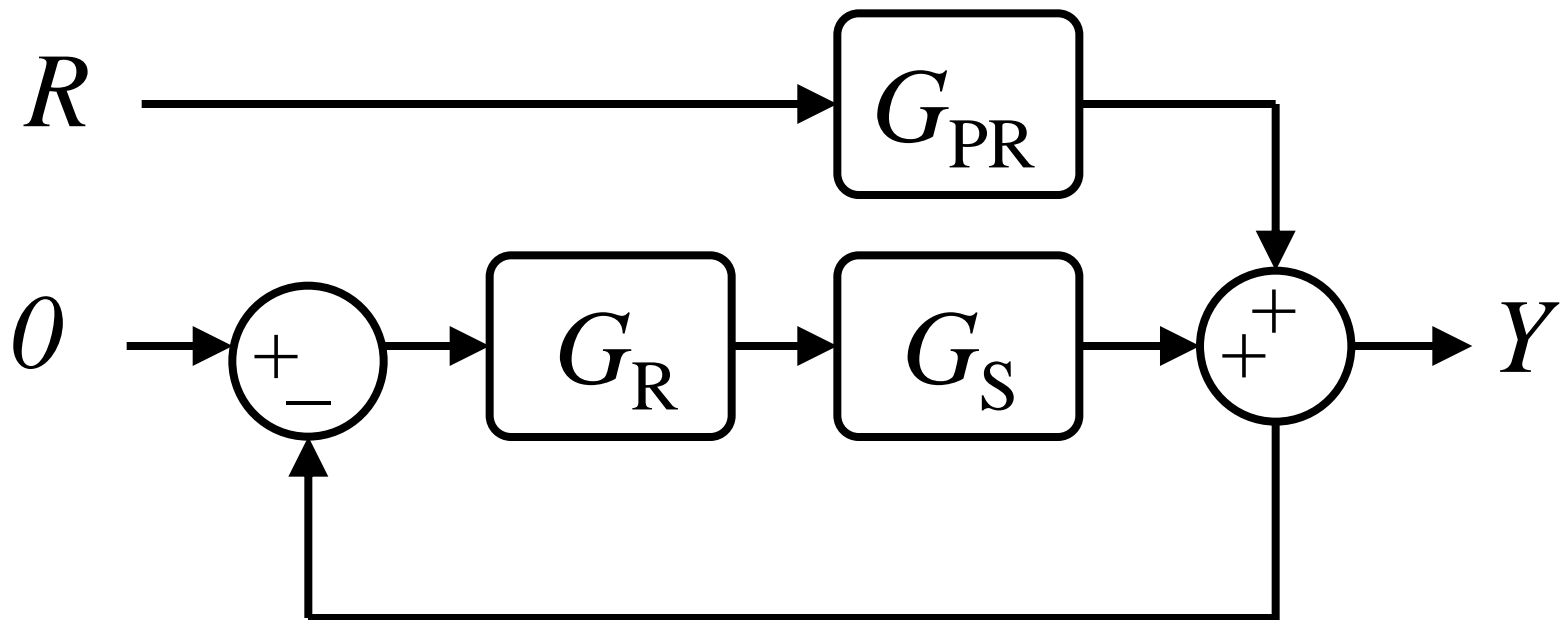
$$R \neq 0$$



# Úloha regulácie

$$W = 0$$

$$R \neq 0$$



# Úloha regulácie

